

## An investigation on the thermodynamic stability of $V_6Si_5$

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Received: 8 May 2007 / Accepted: 18 May 2007 / Published online: 7 June 2007  
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The V–Si system has been assessed by Smith [1, 2], and results were collected in recently published binary phase diagram handbook [3]. The thermodynamic optimizations for the system were also performed by Luoma [4], Rand and Saunders [5]. However, the thermodynamic stability of  $V_6Si_5$  is still in question. Using the method of solid state diffusion, Hallais et al. [6] noted that formation of  $V_6Si_5$  could not be achieved below 1000 °C. By means of bulk V–Si diffusion couples, Milanese et al. [7] found that there is a nucleation barrier for the formation of  $V_6Si_5$  at 1150 °C. Based on the electromotive force (emf) measurement, Eremenko et al. [8] realized that the difficulty of achieving an equilibrium state of V–Si alloys containing the phase  $V_6Si_5$  is indeed overdrawn. Using activity data deduced from the Knudsen cell-mass spectrometry, Storms and Myers [9] indicated the eutectoid decomposition temperature ( $V_6Si_5 \rightleftharpoons V_5Si_3 + VSi_2$ ) as  $1160 \pm 100$  K. This temperature was mistakenly regarded to be 1433 K (1160 °C) in subsequent assessment [2] and thermodynamic optimizations [4, 5]. Here we prepared several alloys in the relevant composition ranges to investigate the thermodynamic stability of  $V_6Si_5$ . Additionally, a combined first-principles/CALPHAD (CALculation of PHase Diagrams) approach is adopted to predict the decomposition temperature and a new set of thermodynamic parameters for vanadium silicides is obtained.

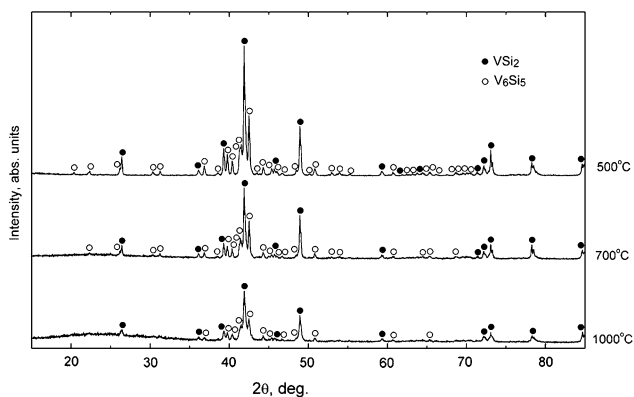
Two alloys ( $V_{41}Si_{59}$  and  $V_{73}Si_{27}$ , in atomic percent) were prepared by arc-melting under argon, with 99.9% purity V and 99.99% purity Si. The alloy  $V_{41}Si_{59}$  was annealed for 2 weeks at both 1000 °C and 700 °C. This temperature range covers the upper and the lower limits of the extrapolated decomposition temperature of  $V_6Si_5$  [9]. The decomposition temperature is calculated to be 573 °C from the Gibbs energy functions assessed by Smith [2]. Therefore, another piece of the alloy  $V_{41}Si_{59}$  was heat-treated at 500 °C for one month. The alloy  $V_{73}Si_{27}$  was put into the same batch at 1000 °C, with a desire to check the possible contamination of interstitial elements. Every alloy was sealed in evacuated silica tubes under vacuum of  $10^{-3}$  bar and then water-quenched after annealing.

To our surprise, the alloys  $V_{41}Si_{59}$  annealed at 1000 °C, 700 °C and 500 °C show a two-phase mixture of  $V_6Si_5$  and  $VSi_2$ , according to X-ray powder diffraction (Fig. 1). This result indicates that the decomposition temperature of  $V_6Si_5$  is below 500 °C. As the diffraction pattern of the alloy  $V_{73}Si_{27}$  show that we obtained  $V_3Si$  plus the tetragonal  $D8_m V_5Si_3$  which will transform to the hexagonal  $D8_8$  with the addition of C, B, N and O [10], therefore, the contamination of interstitial elements is excluded in present experiments.

In order to further determine the relative stability of  $V_6Si_5$  in the  $T = 0$  K ground state, the state-of-art first-principles projector augmented plane-wave (PAW) calculations were applied to all intermetallic compounds of V–Si system using Vienna ab initio simulation package (VASP) [11, 12], together with the Perdew–Burke–Ernzerhof [13] generalized gradient approximation for the exchange–correlation potential. A plane-wave cutoff energy was set to be 400 eV. k-point meshes for Brillouin zone sampling were constructed using the Monkhorst–Pack [14] scheme,

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**Fig. 1** X-ray diffraction patterns of the alloys  $V_{41}Si_{59}$  annealed at 1000 °C, 700 °C for 2 weeks and 500 °C for 1 month. Two-phase mixture of  $VSi_2 + V_6Si_5$  was found in phase identification

and extensive tests were performed (using from  $5 \times 5 \times 5$  to  $15 \times 15 \times 15$  grids). Both the unit cell sizes and the ionic coordinates were fully relaxed to find the stable state. The total energy differences were converged to within 0.1 kJ/mole-atoms.

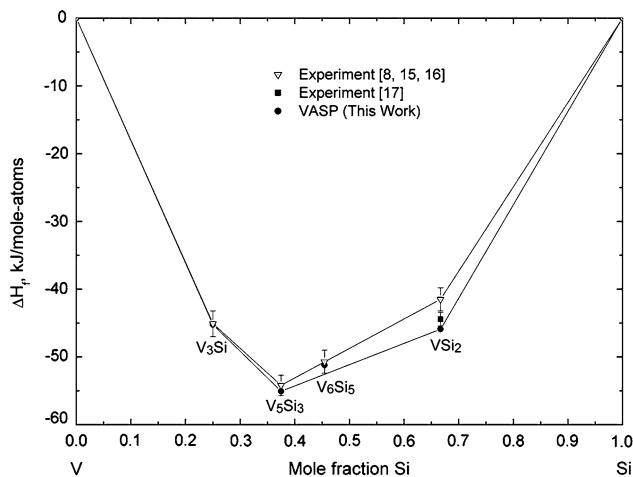
The  $T = 0$  K enthalpy of formation (per atom) of the  $V_pSi_q$  can be calculated from the following equation:

$$\Delta H_f(V_pSi_q) = E(V_pSi_q) - (1 - x)E(V) - xE(Si) \tag{1}$$

where  $E(V)$ ,  $E(Si)$  and  $E(V_pSi_q)$  are the calculated zero-temperature total energies (per atom) of Bcc V, Diamond Si and the corresponding intermetallic phase, respectively, each relaxed to its equilibrium geometry. Here,  $x = q/(p + q)$  is the atomic fraction of Si in these vanadium silicides.

The calculated enthalpies of formation ( $\Delta H_f$ ) are compared with experimental data at room temperature (Fig. 2). Except for  $VSi_2$ , first-principles calculated formation enthalpies agree well with the values measured by Eremenko et al. [8, 15, 16] using emf method. Recently, O’Hare et al. [17] remeasured the enthalpy of formation of  $VSi_2$  by means of fluorine combustion calorimetry. The measured value of O’Hare et al. [17] is very close to the present first-principles calculation. As shown in Fig. 2, first-principles calculated  $\Delta H_f$  of  $V_6Si_5$  falls above the tie-line between those of  $V_5Si_3$  and  $VSi_2$ . This indicates that  $V_6Si_5$  is thermodynamically unstable at  $T = 0$  K and its decomposition temperature is higher.

Due to the formidable computational work at finite-temperature and slow kinetics at low temperatures, an efficiently combined first-principles/CALPHAD hybrid method, which was well illustrated in Al–Sr system by Wolverton et al. [18], is employed to estimate the decomposition temperature of  $V_6Si_5$ . The Gibbs free energy for compound  $V_pSi_q$  is modeled as (J/mole-atoms)



**Fig. 2** First-principles calculated enthalpies of formation for the compounds in the V–Si system, compared with the experimental data of Eremenko et al. [8, 15, 16] and O’Hare et al. [17]

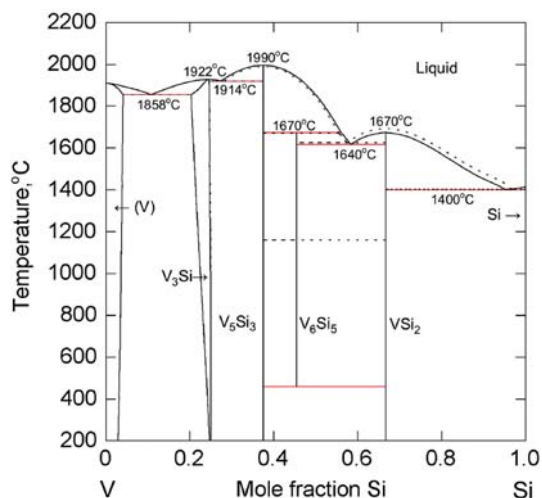
$$G^{V_pSi_q} = (1 - x)^oG_V + x^oG_{Si} + a + bT \tag{2}$$

where  $^oG_V$  and  $^oG_{Si}$  is the molar Gibbs energy of pure V and Si in their stable structure at room temperature [19]. Accepting the parameters for liquid phase evaluated by Luoma [4], we optimized the parameters  $a$  and  $b$  for  $VSi_2$ ,  $V_6Si_5$  and  $V_5Si_3$  respectively using the information on the congruent melting points and the invariant reactions [2]. The calculated enthalpies of formation at  $T = 0$  K are set as the starting values for parameter  $a$  and limited to vary within  $\pm 1$  kJ, which is the typical accuracy of first-principles calculations. All parameters generated in this work are listed in Table 1.

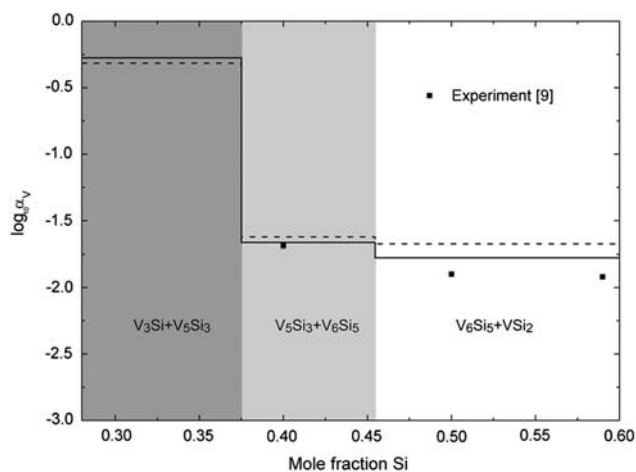
The general agreement between the calculated phase diagram in this work and that of Luoma [4] is excellent (Fig. 3). The decomposition temperature of  $V_6Si_5$  is predicted to be 460 °C which is consistent with the present experimental result. Lozova et al. [20] did not find  $V_6Si_5$  in the presented isothermal section of the Li–V–Si system at 297 °C. Thus the real decomposition temperature of the  $V_6Si_5$  should be between 297 °C and 460 °C. Moreover, the predicted phase stability diagram using the present parameters is in good agreement with the experimental data reported by Storms and Myers [9] (Fig. 4). This is another check of the reliability of the presently obtained parameters.

**Table 1** The optimized parameters for vanadium silicides based on the output of first-principles calculations and experimental phase diagram data

Phase	Eq. (2) a (J/mole-atoms)	Eq. (2) b (J/mole-atoms·K)
$VSi_2$	–45913.1	3.79418
$V_6Si_5$	–52220.5	4.44687
$V_5Si_3$	–55072.0	5.35583



**Fig. 3** Comparison between the calculated V–Si phase diagram of Luoma [4] (dash line) and the present work (solid line)



**Fig. 4** Model-predicted phase stability diagram at 1650 K, compared with the experimental data of Storms and Myers [9]. (Dash line is calculated using the parameters of Luoma [4] and solid line comes from the present work).  $a_v$  is the activity of Vanadium. The reference state is bcc-V

The combined CALPHAD/first-principles approach shows its value to detect the eutectoid decomposition temperature of  $V_6Si_5$ , which is confirmed experimentally to

be stable down to 500 °C. The newly obtained parameters for the vanadium silicides provide a more precise description of the thermodynamic stability of  $V_6Si_5$ .

**Acknowledgements** The financial supports from the National Outstanding Youth Science Foundation of China (Grant No. 50425103), Hunan Provincial Natural Science Foundation of China (Grant No. 06JJ20010) and the State Key Laboratory of High Performance Ceramics and Superfine Microstructure, Shanghai Institute of Ceramics (Grant No. SKL200606SIC) are acknowledged.

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